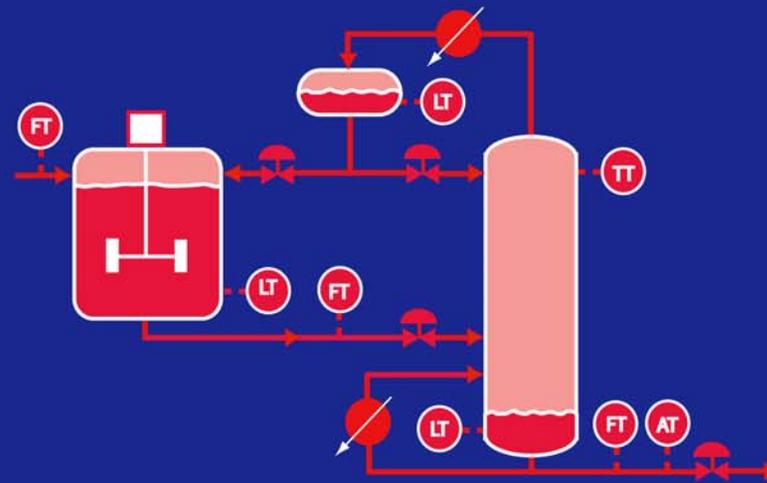


# Process Dynamics and Control

Second Edition



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# Process Dynamics

- a) Refers to unsteady-state or transient behavior.
- b) Steady-state vs. unsteady-state behavior
  - i. Steady state: variables do not change with time
  - ii. But on what scale? cf., noisy measurement
- c) ChE curriculum emphasizes steady-state or equilibrium situations:
  - i. Examples: ChE 10, 110, 120.
- d) *Continuous processes*: Examples of transient behavior:
  - i. Start up & shutdown
  - ii. Grade changes
  - iii. Major disturbance: e.g., refinery during stormy or hurricane conditions
  - iv. Equipment or instrument failure (e.g., pump failure)

- e) *Batch processes*
  - i. Inherently unsteady-state operation
  - ii. Example: Batch reactor
    - 1. Composition changes with time
    - 2. Other variables such as temperature could be constant.

## Process Control

- a) Large scale, continuous processes:
  - i. Oil refinery, ethylene plant, pulp mill
  - ii. Typically, 1000 – 5000 process variables are measured.
    - 1. Most of these variables are also controlled.

## Process Control (cont'd.)

iii. Examples: flow rate,  $T$ ,  $P$ , liquid level, composition

iv. Sampling rates:

1. Process variables: A few seconds to minutes

2. Quality variables: once per 8 hr shift, daily, or weekly

b) Manipulated variables

i. We implement “process control” by manipulating process variables, usually flow rates.

1. Examples: feed rate, cooling rate, product flow rate, etc.

ii. Typically, several thousand manipulated variables in a large continuous plant

## Process Control (cont'd.)

c) Batch plants:

i. Smaller plants in most industries

1. Exception: microelectronics (200 – 300 processing steps).

ii. But still large numbers of measured variables.

d) Question: How do we control processes?

i. We will consider an illustrative example.

## 1.1 Illustrative Example: Blending system

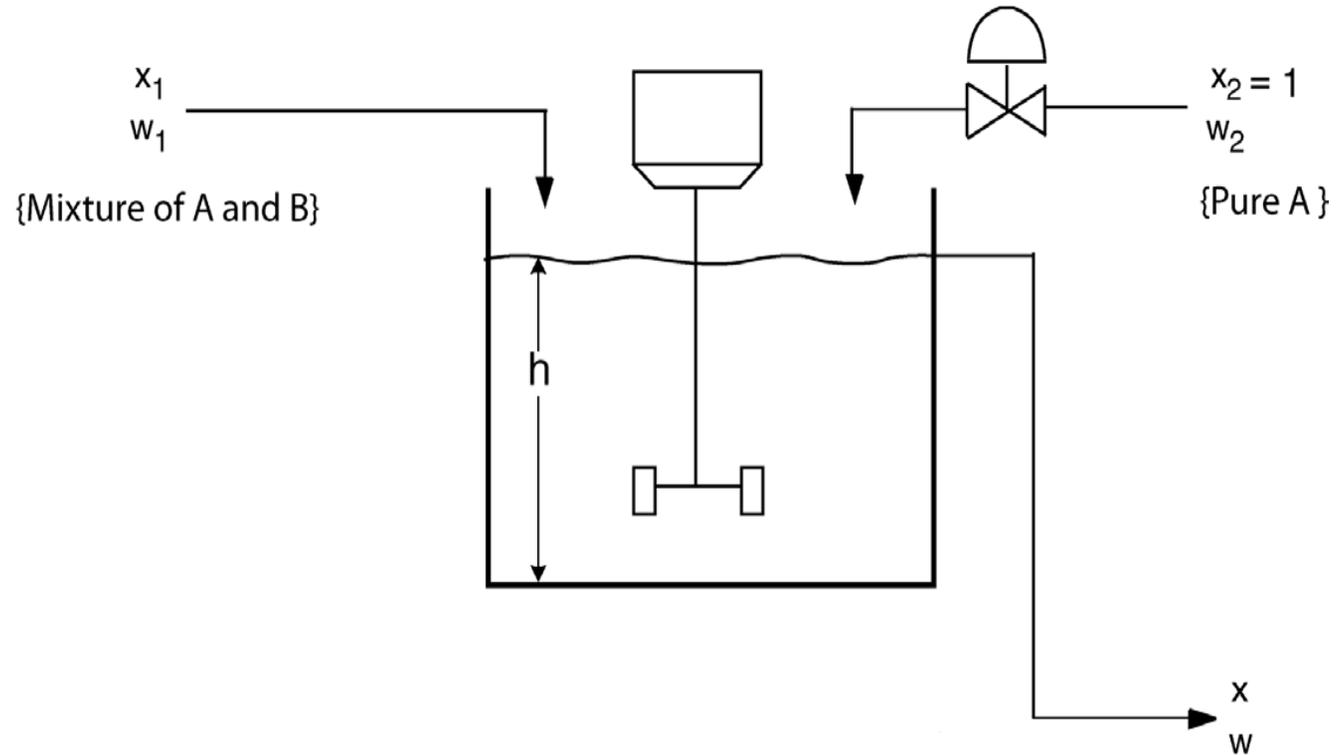


Figure 1.3. Stirred-tank blending system.

### Notation:

- $w_1$ ,  $w_2$  and  $w$  are mass flow rates
- $x_1$ ,  $x_2$  and  $x$  are mass fractions of component A

**Assumptions:**

1.  $w_1$  is constant
2.  $x_2 = \text{constant} = 1$  (stream 2 is pure A)
3. Perfect mixing in the tank

**Control Objective:**

Keep  $x$  at a desired value (or “set point”)  $x_{sp}$ , despite variations in  $x_1(t)$ . Flow rate  $w_2$  can be adjusted for this purpose.

**Terminology:**

- Controlled variable (or “output variable”):  $x$
- Manipulated variable (or “input variable”):  $w_2$
- Disturbance variable (or “load variable”):  $x_1$

**Design Question.** What value of  $\bar{w}_2$  is required to have  $\bar{x} = x_{SP}$ ?

**Overall balance:**

$$0 = \bar{w}_1 + \bar{w}_2 - \bar{w} \quad (1-1)$$

**Component A balance:**

$$\bar{w}_1 \bar{x}_1 + \bar{w}_2 \bar{x}_2 - \bar{w} \bar{x} = 0 \quad (1-2)$$

(The overbars denote nominal steady-state design values.)

- At the design conditions,  $\bar{x} = x_{SP}$ . Substitute Eq. 1-2,  $\bar{x} = x_{SP}$  and  $\bar{x}_2 = 1$ , then solve Eq. 1-2 for  $\bar{w}_2$ :

$$\bar{w}_2 = \bar{w}_1 \frac{x_{SP} - \bar{x}_1}{1 - x_{SP}} \quad (1-3)$$

- Equation 1-3 is the design equation for the blending system.
- If our assumptions are correct, then this value of  $\bar{w}_2$  will keep  $\bar{x}$  at  $x_{SP}$ . But what if conditions change?

***Control Question.*** Suppose that the inlet concentration  $x_1$  changes with time. How can we ensure that  $x$  remains at or near the set point  $x_{SP}$ ?

As a specific example, if  $x_1 > \bar{x}_1$  and  $w_2 = \bar{w}_2$ , then  $x > x_{SP}$ .

## Some Possible Control Strategies:

**Method 1.** Measure  $x$  and adjust  $w_2$ .

- Intuitively, if  $x$  is too high, we should reduce  $w_2$ ;

- Manual control vs. automatic control
- Proportional feedback control law,

$$w_2(t) = \bar{w}_2 + K_c [x_{SP} - x(t)] \quad (1-4)$$

1. where  $K_c$  is called the controller gain.
2.  $w_2(t)$  and  $x(t)$  denote variables that change with time  $t$ .
3. The change in the flow rate,  $w_2(t) - \bar{w}_2$ , is proportional to the deviation from the set point,  $x_{SP} - x(t)$ .

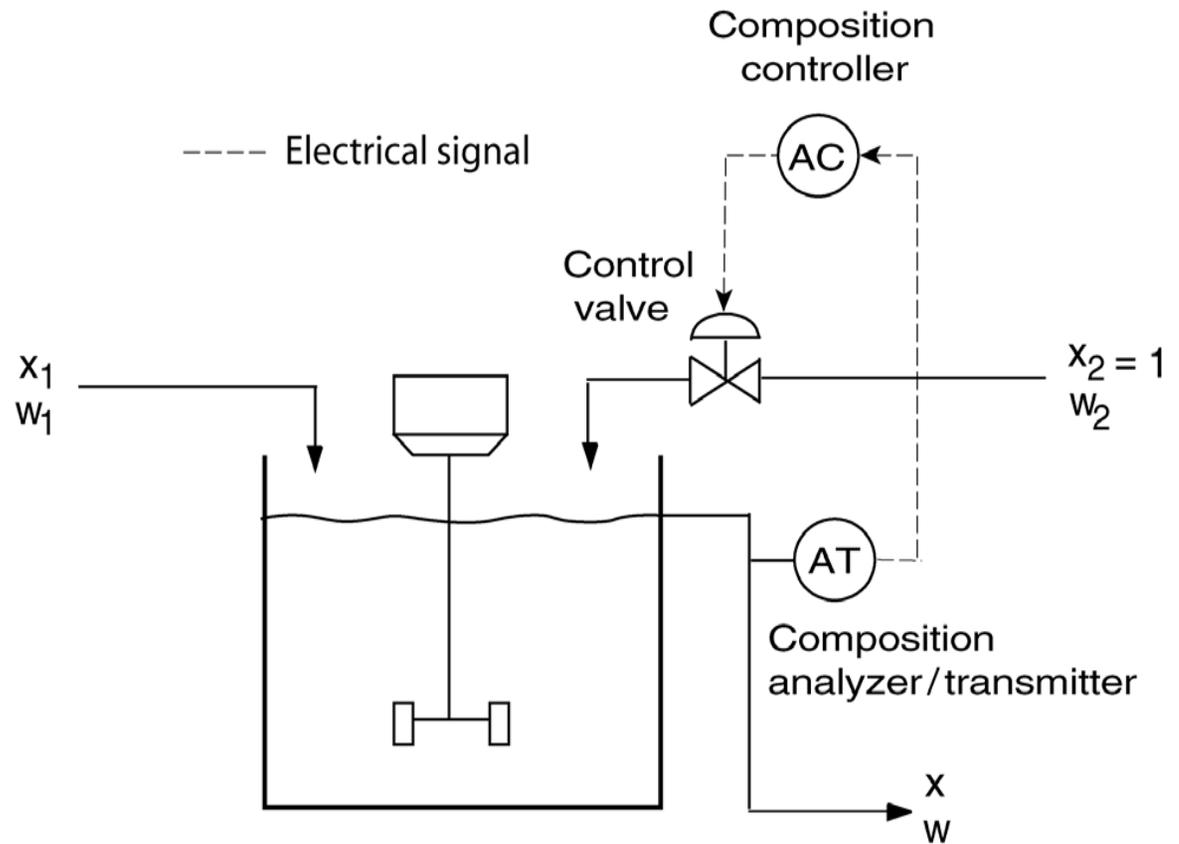


Figure 1.4. Blending system and Control Method 1.

**Method 2.** *Measure  $x_1$  and adjust  $w_2$ .*

- Thus, if  $x_1$  is greater than  $\bar{x}_1$ , we would decrease  $w_2$  so that  $w_2 < \bar{w}_2$ ;
- **One approach:** Consider Eq. (1-3) and replace  $\bar{x}_1$  and  $\bar{w}_2$  with  $x_1(t)$  and  $w_2(t)$  to get a control law:

$$w_2(t) = \bar{w}_1 \frac{x_{SP} - x_1(t)}{1 - x_{SP}} \quad (1-5)$$

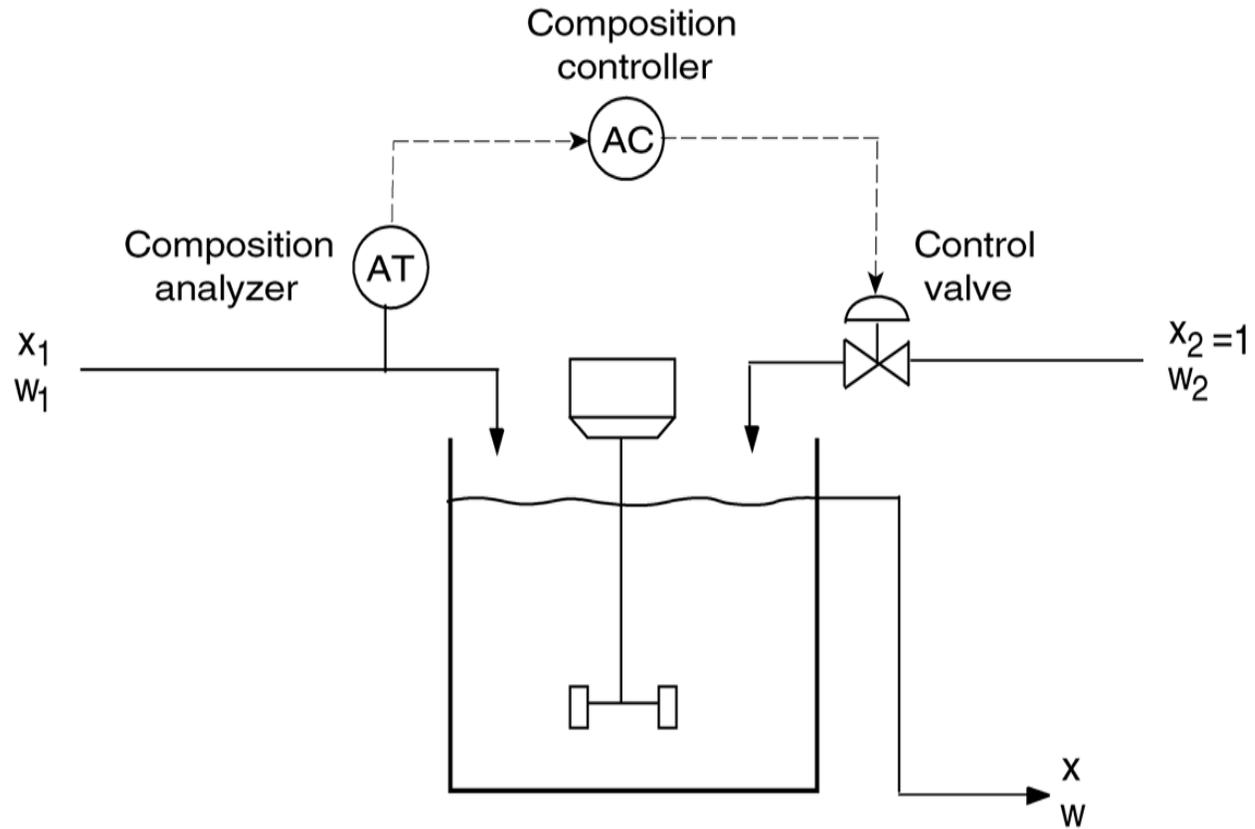


Figure 1.5. Blending system and Control Method 2.

- Because Eq. (1-3) applies only at steady state, it is not clear how effective the control law in (1-5) will be for transient conditions.

**Method 3.** *Measure  $x_1$  and  $x$ , adjust  $w_2$ .*

- This approach is a combination of Methods 1 and 2.

**Method 4.** *Use a larger tank.*

- If a larger tank is used, fluctuations in  $x_1$  will tend to be damped out due to the larger capacitance of the tank contents.
- However, a larger tank means an increased capital cost.

## 1.2 Classification of Control Strategies

Table. 1.1 Control Strategies for the Blending System

<i>Method</i>	<i>Measured Variable</i>	<i>Manipulated Variable</i>	<i>Category</i>
1	$x$	$w_2$	FB <sup>a</sup>
2	$x_1$	$w_2$	FF
3	$x_1$ and $x$	$w_2$	FF/FB
4	-	-	Design change

### Feedback Control:

- **Distinguishing feature:** measure the controlled variable

- It is important to make a distinction between *negative feedback* and *positive feedback*.

- Engineering Usage vs. Social Sciences

- **Advantages:**

- Corrective action is taken regardless of the source of the disturbance.
- Reduces sensitivity of the controlled variable to disturbances and changes in the process (shown later).

- **Disadvantages:**

- No corrective action occurs until after the disturbance has upset the process, that is, until after  $x$  differs from  $x_{sp}$ .
- Very oscillatory responses, or even instability...

## Feedforward Control:

- Distinguishing feature: measure a disturbance variable
- **Advantage:**
  - Correct for disturbance before it upsets the process.
- **Disadvantage:**
  - Must be able to measure the disturbance.
  - No corrective action for unmeasured disturbances.

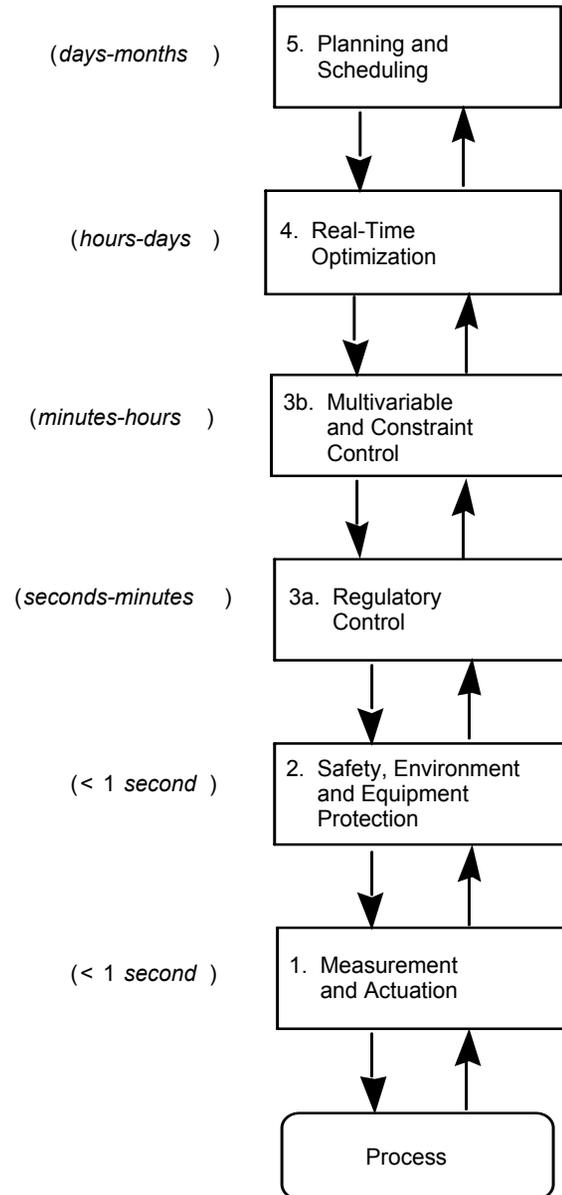


Figure 1.7 Hierarchy of process control activities.

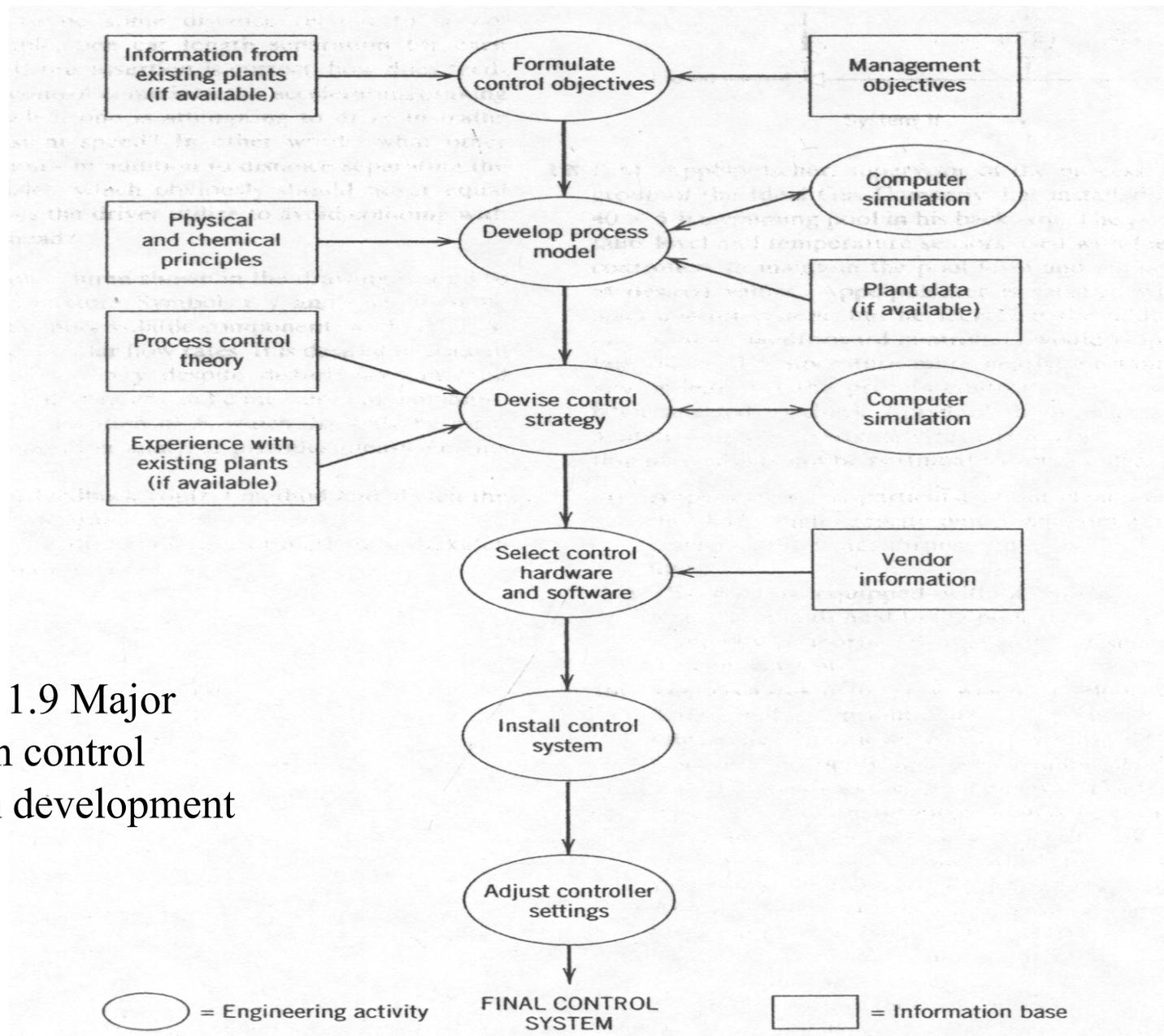


Figure 1.9 Major steps in control system development